



Exam IV

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Enter Name:

I.D. Number:

Answer each of the following. Passing is 100%.

1. The sequence
$$\left\{\frac{n}{n+1}\right\}_{n=1}^{\infty}$$
 is

Increasing Not bounded Not monotone Decreasing

2. The series
$$\sum_{n=0}^{\infty} \frac{\ln n}{n^3}$$
 is

Diverges by Comparison Test

Converges by Comparison Test Diverges by Integral Test

Converges by Ratio Test

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Test

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3. The series
$$\sum_{n=0}^{\infty} \frac{\sqrt{n}}{\ln n}$$
 is

Converges by Comparison Test Converges by Integral Test

4. The series
$$\sum_{n=1}^{\infty} \frac{10}{n(n+1)}$$
 is

Divergent Convergent to 0 Convergent to -10Convergent to 10

Converges by Ratio Test

Diverges by Comparison

5. The radius of convergence of the power series $\sum_{n=0}^{\infty} \frac{(-1)^n (x-3)^n}{n+1}$ is

$$\begin{array}{l} R=\infty & R=3 \\ R=4 & R=1 \end{array}$$

6. The sequence $\{-1, 0, 1, -1, 0, 1, -1, 0, 1, \ldots\}$ is

Convergent to 0	Convergent to 1
Divergent	Convergent to -1

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7. The sequence
$$\left\{ \left(\frac{1}{n}\right)^{1/\ln n} \right\}_{n=1}^{\infty}$$
 is
Divergent Convergent to 1
Convergent to e Convergent to -1
8. The series $\sum_{n=0}^{\infty} \frac{\sin n}{3^n}$ is
Diverges Absolutely Convergent
Conditionally Convergent
Convergent
9. The series $\sum_{n=0}^{\infty} \frac{n2^n}{3^n}$ is
Diverges by Comparison Converges by Integral
Test Test
Diverges by Comparison Converges by Ratio Test
Test

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10. The series
$$\sum_{n=0}^{\infty} \frac{n2^n}{3^n}$$
 is
Diverges by Comparison Diverges by Root Test
Test
Converges by Integral Converges by Root Test
Test
11. The sequence $\left\{\frac{n}{n+1}\right\}_{n=1}^{\infty}$ is
Not monotone Not bounded
Divergent Bounded
12. The interval of convergence of the power series $\sum_{n=0}^{\infty} \frac{(-1)^n (x-3)^n}{n+1}$
is
 $\begin{bmatrix} 2,4 \\ (2,4 \end{bmatrix}$ $\begin{bmatrix} 2,4 \\ (2,4 \end{bmatrix}$

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13. The series
$$\sum_{n=0}^{\infty} \frac{n+2}{3n-1}$$
 is

Converges by Integral Test

Converges by Comparison Test Diverges by Divergence Test Diverges by Ratio Test

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14. The Taylor series for $f(x) = \ln x$ at a = 2 is

$$\frac{\ln 2 + \sum_{n=0}^{\infty} \frac{(-1)^{n+1} (x-2)^{n+1}}{(n+1)2^{n+1}}}{\sum_{n=0}^{\infty} \frac{(-1)^{n+1} (x-2)^{n+1}}{(n+1)2^{n+1}}} = \frac{1 + \sum_{n=1}^{\infty} \frac{(-1)^n (x-2)^{n+1}}{(n+1)2^{n+1}}}{\sum_{n=0}^{\infty} \frac{(-1)^{n+1} (x-2)^{n+1}}{(n+1)2^{n+1}}} = \frac{\ln 2 + \sum_{n=1}^{\infty} \frac{(-1)^n (x-2)^{n+1}}{(n+1)2^{n+1}}}{(n+1)2^{n+1}}$$
15. The sequence $\left\{\frac{(-1)^n n}{n+1}\right\}_{n=1}^{\infty}$ is
Convergent to -1 Convergent to 1
Convergent to 0 Divergent

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16. The sum of the series $\sum_{n=0}^{\infty} \frac{\cos(n\pi)}{3^n}$ is $\frac{-1}{3}$ -3 $\frac{3}{4}$ $\frac{1}{3}$ 17. $\lim_{n \to \infty} \tanh n =$ $\pi/2$ 1 DNE **18.** The sum of the series $\sum_{n=1}^{\infty} \left(\frac{1}{\sqrt{n}} - \frac{1}{\sqrt{n+1}} \right)$ is $\sqrt{2}$ -10 **19.** The series $\sum_{n=0}^{\infty} \frac{2^n + 3^n}{5^n + 2}$ is Converges by Integral Converges by Test Comparison Test Diverges by Comparison Converges by Ratio Test Test

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20. The power series for $f(x) = \sin^2 x$ is

$$\sum_{n=0}^{\infty} \frac{(-1)^{n+1} 2^{2n-1} x^{2n}}{(2n)!} \qquad 1 + \sum_{n=1}^{\infty} \frac{(-1)^n 2^{2n-1} x^{2n+1}}{(2n+1)!} \\ 1 + \sum_{n=0}^{\infty} \frac{(-1)^n 2^{2n-1} x^{2n+1}}{(2n+1)!} \qquad \sum_{n=1}^{\infty} \frac{(-1)^{n+1} 2^{2n-1} x^{2n}}{(2n)!}$$

Answers:

Points:

Percent:

Letter Grade: