

ABET OCs	A	G	K
Question No.	Q1-a, Q2-a,b	-	Q1-b

50
50
Excellent

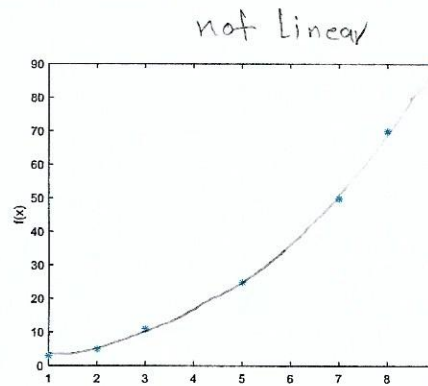
From the given data shown in table and graph below:

- Q1. (a) Find the regression model using **Least Square Error Criterion** with **appropriate order**. (15 marks)
(b) Write MATLAB code for regression the data with your approximate **polynomial** model. Show in your code computed error. (10 marks)

Q2. Interpolate the data (at $x=4$) using the following methods:

- (a) **Lagrange** interpolation method (15 marks)
(b) **Newton's divided difference** interpolation method (15 marks)

x	f(x)
1	3
2	5
3	11
5	25
7	50
8	70
10	90



$$\text{slop} = \frac{2^x - 1}{5 - 3} = \frac{1}{2} \quad \text{and} \quad \frac{5 - 3}{25 - 11} = \frac{1}{7}$$

$$\frac{10 - 7}{90 - 50} = \frac{3}{40}$$

$$Y = a_0 + a_1 X + a_2 X^2$$

$$\sum x_i = 36, \quad \sum x_i^2 = 252, \quad \sum x_i^3 = 2016$$

$$\sum x_i^4 = 17220; \quad n = 7, \quad \sum f(x) = 254$$

$$\sum x_i f(x) = 1981, \quad \sum x_i^2 f(x) = 16677$$

$$\begin{bmatrix} n & \sum(x_i) & \sum(x_i)^2 \\ \sum(x_i) & \sum(x_i)^2 & \sum(x_i)^3 \\ \sum(x_i)^2 & \sum(x_i)^3 & \sum(x_i)^4 \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ a_2 \end{bmatrix} = \begin{bmatrix} \sum f(x) \\ \sum x_i f(x) \\ \sum x_i^2 f(x) \end{bmatrix}$$

$$\therefore 7 a_0 + 36 a_1 + 252 a_2 = 254$$

$$36 a_0 + 252 a_1 + 2016 a_2 = 1981$$

$$252 a_0 + 2016 a_1 + 17220 a_2 = 16677$$

$$\therefore a_0 = -2.49, \quad a_1 = 2.8, \quad a_2 = 0.677$$

(b)

$$X = [1 \quad 2 \quad 3 \quad 5 \quad 7 \quad 8 \quad 10];$$

$$Y = [3 \quad 5 \quad 11 \quad 25 \quad 50 \quad 70 \quad 90];$$

$$A = \text{polyfit}(X, Y, 2);$$

$$B = \text{fliplr}(A);$$

Q2)

$4 + x = 4$

a) Lagrange method

$$f(x) = L_0 \overset{5}{F(x_0)} + L_1 \overset{11}{(F x_1)} + L_2 \overset{25}{(F x_2)}$$

$$L_0 = \left(\frac{x - x_1}{x_0 - x_1} \right) \left(\frac{x - x_2}{x_0 - x_2} \right)$$

$$L_1 = \left(\frac{x - x_0}{x_1 - x_0} \right) \left(\frac{x - x_2}{x_1 - x_2} \right)$$

$$L_2 = \left(\frac{x - x_0}{x_2 - x_0} \right) \left(\frac{x - x_1}{x_2 - x_1} \right)$$

$$x_0 = 2 \Rightarrow F(x_0) = 5$$

$$x_1 = 3 \Rightarrow F(x_1) = 11$$

$$x_2 = 5 \Rightarrow F(x_2) = 25$$

$$f(4) = \left(\frac{4-3}{2-3} \right) \left(\frac{4-5}{2-5} \right) (5) + \left(\frac{4-2}{3-2} \right) \left(\frac{4-5}{3-5} \right) (11)$$

$$+ \left(\frac{4-2}{5-2} \right) \left(\frac{4-3}{5-3} \right) (25) = 17.67$$

$4 + x = 4$

b) Newton's method

$$b_0 + b_1(x - x_0) + b_2(x - x_0)(x - x_1)$$

$$b_0 = f(x_0)$$

$$b_1 = \frac{f(x_1) - f(x_0)}{x_1 - x_0}$$

$$b_2 = \frac{\frac{f(x_2) - f(x_1)}{x_2 - x_1} - \frac{f(x_1) - f(x_0)}{x_1 - x_0}}{x_2 - x_0}$$

$$x_0 = 2 \Rightarrow f(x_0) = 5$$

$$x_1 = 3 \Rightarrow f(x_1) = 11$$

$$x_2 = 5 \Rightarrow f(x_2) = 25$$

$$b_0 = f(x_0) = f(2) = 5$$

$$b_1 = \frac{11 - 5}{3 - 2} = 6$$

$$b_2 = \frac{\frac{25 - 11}{5 - 3} - \frac{11 - 5}{3 - 2}}{5 - 2} = \frac{1}{3}$$

$$f(4) = 5 + 6(4 - 2) + \frac{1}{3}(4 - 2)(4 - 3)$$

$$= 17.67$$