## ELectric Charge

- Electric charge is an intrinsic property of particles, such as electrons and protons.
- There are two types of charges: positive and negatives.
- Electrons have a negative charge.
- Protons have a positive charge.
- Charged particles can interact to create an electrical force.
- Similar charges produce a repulsive force, where each one repels the other.
- Dissimilar charges produce an attractive force, where each one attracts the other.


## Glass + silk = + charge


(a)

## Plastic+ fur $=$ - charge

(b)

Charges with the same electrical sign repel each other, and charges with opposite electrical signs attract each other.

## CONDUCTORS AND INSULATORS

- Materials are classified into four categories in terms of their capability of conducting electricity.
- Insulators: materials that a significant amount of electrons are not free to move. examples include rubber plastic, glass, and chemically pure water.
- Conductors: materials that a significant amount of electrons are free to move ( rather freely); examples include metals (such as copper in common lamp wire.
- Semiconductors: materials that sometimes behave like insulators and sometimes behave like conductors, intermediate between conductors and insulators. ; examples include silicon and germanium in computer chips
- Superconductors: materials that almost all electrons are free to move, perfect conductors(allowing charge to move without any hindrance).


## QUANTIZATION OF CHARGE

Th
the Coulomb (C) is the SI unit of charge.
Any electric charge $(q)$ is quantized, that means it depends on the number of electrons $(n)$, according to

$$
q=n e
$$

The electric current is the rate of change of the electric charge

$$
i=\frac{d q}{d t}
$$

Therefore , 1 Coulomb (C) = 1 Ampere (A). 1 second ( s ).

## ELECTROSTATIC FORCE - COULOMB's LAW

The magnitude of the electrostatic force (attractive or repulsive) between two charged particles $q_{1}$ and $q_{2}$ separated by a distance $r$ is determined hv

$$
F=\frac{k\left|q_{1}\right|\left|q_{2}\right|}{r^{2}}
$$

where $k$ is a constant equals to $9.0 \times 10^{9} \mathrm{~N} . \mathrm{m}^{2} / \mathrm{C}^{2}$, whi

$$
k=\frac{1}{4 \pi \varepsilon_{0}}
$$

(a)


The electric force is a vector quantity, therefore the resultant force on a

where $\varepsilon_{0}$ is known as the permittivity and equals to 8.8 . superposition vector of all forces acting on :

$$
\vec{F}_{1, \text { net }}=\vec{F}_{12}+\vec{F}_{13}+\vec{F}_{14}+\vec{F}_{15}+\cdots+\vec{F}_{1 n},
$$

## Sample Problem

(a) Figure 21-9a shows two positively charged particles fixed in place on an $x$ axis. The charges are $q_{1}=1.60 \times$

(b)

Figure 21-9a

Two particles: Using Eq. 21-4 with separation $R$ substituted for $r$, we can write the magnitude $F_{12}$ of this force as

$$
\begin{aligned}
F_{12}= & \frac{1}{4 \pi \varepsilon_{0}} \frac{\left|q_{1}\right|\left|q_{2}\right|}{R^{2}} \\
= & \left(8.99 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}\right) \\
& \times \frac{\left(1.60 \times 10^{-19} \mathrm{C}\right)\left(3.20 \times 10^{-19} \mathrm{C}\right)}{(0.0200 \mathrm{~m})^{2}} \\
= & 1.15 \times 10^{-24} \mathrm{~N}
\end{aligned}
$$

Thus, force $\vec{F}_{12}$ has the following magnitude and direction (relative to the positive direction of the $x$ axis):

$$
1.15 \times 10^{-24} \mathrm{~N} \text { and } 180^{\circ} . \quad \text { (Answer) }
$$

We can also write $\vec{F}_{12}$ in unit-vector notation as

$$
\vec{F}_{12}=-\left(1.15 \times 10^{-24} \mathrm{~N}\right) \hat{\mathrm{i}} . \quad(\text { Answer })
$$

(b) Figure $21-9 c$ is identical to Fig. $21-9 a$ except that particle 3 now lies on the $x$ axis between particles 1 and 2. Particle 3 has charge $q_{3}=-3.20 \times 10^{-19} \mathrm{C}$ and is at a distance $\frac{3}{4} R$ from particle 1 . What is the net electrostatic force $\vec{F}_{1 . \text { net }}$ on particle 1 due to particles 2 and 3 ?

(c)

(d)

Figure 21-9c
Three particles: To find the magnitude of $\vec{F}_{13}$, we can rewrite Eq. 21-4 as

$$
\begin{aligned}
F_{13}= & \frac{1}{4 \pi \varepsilon_{0}} \frac{\left|q_{1}\right|\left|q_{3}\right|}{\left(\frac{3}{4} R\right)^{2}} \\
= & \left(8.99 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}\right) \\
& \times \frac{\left(1.60 \times 10^{-19} \mathrm{C}\right)\left(3.20 \times 10^{-19} \mathrm{C}\right)}{\left(\frac{3}{4}\right)^{2}(0.0200 \mathrm{~m})^{2}} \\
= & 2.05 \times 10^{-24} \mathrm{~N} .
\end{aligned}
$$

We can also write $\vec{F}_{13}$ in unit-vector notation:

$$
\begin{aligned}
& \vec{F}_{13}=\left(2.05 \times 10^{-24} \mathrm{~N}\right) \hat{\mathrm{i}} \\
\vec{F}_{1, \text { net }} & =\vec{F}_{12}+\vec{F}_{13} \\
= & -\left(1.15 \times 10^{-24} \mathrm{~N}\right) \hat{\mathrm{i}}+\left(2.05 \times 10^{-24} \mathrm{~N}\right) \hat{\mathrm{i}} \\
= & \left(9.00 \times 10^{-25} \mathrm{~N}\right) \hat{\mathrm{i}}
\end{aligned}
$$

Thus, $\vec{F}_{1, \text { net }}$ has the following magnitude and direction (relative to the positive direction of the $x$ axis):

$$
9.00 \times 10^{-25} \mathrm{~N} \quad \text { and } 0^{\circ} .
$$

(c) Figure $21-9 e$ is identical to Fig. 21-9a except that particle 4 is now included. It has charge $q_{4}=-3.20 \times 10^{-19} \mathrm{C}$, is at a distance $\frac{3}{4} R$ from particle 1 , and lies on a line that makes an angle $\theta=60^{\circ}$ with the $x$ axis. What is the net electrostatic force $\vec{F}_{1, \text { net }}$ on particle 1 due to particles 2 and 4 ?

Summing components axis by axis. The sum of the $x$ components gives us

$$
\begin{aligned}
F_{1, \text { net }, x} & =F_{12, x}+F_{14, x}=F_{12}+F_{14} \cos 60^{\circ} \\
& =-1.15 \times 10^{-24} \mathrm{~N}+\left(2.05 \times 10^{-24} \mathrm{~N}\right)\left(\cos 60^{\circ}\right) \\
& =-1.25 \times 10^{-25} \mathrm{~N}
\end{aligned}
$$


(e)


Figure 21-9e

The sum of the $y$ components gives us

$$
\begin{aligned}
F_{1, \text { net }, y} & =F_{12, y}+F_{14, y}=0+F_{14} \sin 60^{\circ} \\
& =\left(2.05 \times 10^{-24} \mathrm{~N}\right)\left(\sin 60^{\circ}\right)
\end{aligned}
$$

The net force $\vec{F}_{1, \text { net }}$ has the magnitude

$$
F_{1, \text { net }}=\sqrt{F_{1, \text { net }, x}^{2}+F_{1, \text { net, }, y}^{2}}=1.78 \times 10^{-24} \mathrm{~N} . \text { (Answer) }
$$

To find the direction of $\vec{F}_{1 \text {,net }}$, we take

$$
\theta=\tan ^{-1} \frac{F_{1, \text { net }, y}}{F_{1, \text { net }, x}}=-86.0^{\circ}
$$

Method 3. Summing components axis by axis. The sum
of the $x$ components gives us

$$
\begin{aligned}
F_{1, \text { net }, x} & =F_{12, x}+F_{14, x}=F_{12}+F_{14} \cos 60^{\circ} \\
& =-1.15 \times 10^{-24} \mathrm{~N}+\left(2.05 \times 10^{-24} \mathrm{~N}\right)\left(\cos 60^{\circ}\right) \\
& =-1.25 \times 10^{-25} \mathrm{~N} .
\end{aligned}
$$

The sum of the $y$ components gives us

$$
\begin{aligned}
F_{1, \text { net }, y} & =F_{12, y}+F_{14, y}=0+F_{14} \sin 60^{\circ} \\
& =\left(2.05 \times 10^{-24} \mathrm{~N}\right)\left(\sin 60^{\circ}\right) \\
& =1.78 \times 10^{-24} \mathrm{~N} .
\end{aligned}
$$

The net force $\vec{F}_{1, \text { net }}$ has the magnitude

$$
F_{1, \text { net }}=\sqrt{F_{1, \text { net }, x}^{2}+F_{1, \text { net }, y}^{2}}=1.78 \times 10^{-24} \mathrm{~N} . \quad \text { (Answer) }
$$

To find the direction of $\vec{F}_{1, \text { net }}$, we take

$$
\theta=\tan ^{-1} \frac{F_{1, \text { net }, y}}{F_{1, \text { net }, x}}=-86.0^{\circ}
$$

\section*{| Sample Problem | $21-2$ |
| :--- | :--- |}

Figure 21-10a shows two particles fixed in place: a particle of charge $q_{1}=+8 q$ at the origin and a particle of charge $q_{2}=$ $-2 q$ at $x=L$. At what point (other than infinitely far away) can a proton be placed so that it is in equilibrium (the net force on it is zero)? Is that equilibrium stable or unstable?



## KEY IDEA If $\vec{F}_{1}$ is the force on the proton due to charge

(b)

(d) $q_{1}$ and $\vec{F}_{2}$ is the force on the proton due to charge $q_{2}$, then the point we seek is where $\vec{F}_{1}+\vec{F}_{2}=0$. Thus,

$$
\begin{equation*}
\vec{F}_{1}=-\vec{F}_{2} . \tag{21-8}
\end{equation*}
$$

This tells us that at the point we seek, the forces acting on the proton due to the other two particles must be of equal magnitudes,

$$
\begin{equation*}
F_{1}=F_{2}, \tag{21-9}
\end{equation*}
$$

and that the forces must have opposite directions.

Calculations: With the aid of Eq. 21-4, we can now rewrite Eq. 21-9 (which says that the forces have equal magnitudes):

$$
\begin{equation*}
\frac{1}{4 \pi \varepsilon_{0}} \frac{8 q q_{\mathrm{p}}}{x^{2}}=\frac{1}{4 \pi \varepsilon_{0}} \frac{2 q q_{\mathrm{p}}}{(x-L)^{2}} \tag{21-10}
\end{equation*}
$$

(Note that only the charge magnitudes appear in Eq. 21-10.) Rearranging Eq. 21-10 gives us

$$
\begin{aligned}
& \left(\frac{x-L}{x}\right)^{2}=\frac{1}{4} \\
& \frac{x-L}{x}=\frac{1}{2}, \\
& x=2 L .
\end{aligned}
$$

(Answer)

## Sample Problem

The nucleus in an iron atom has a radius of about $4.0 \times$ $10^{-15} \mathrm{~m}$ and contains 26 protons.
(a) What is the magnitude of the repulsive electrostatic force between two of the protons that are separated by $4.0 \times 10^{-15} \mathrm{~m}$ ?

Calculation: Table 21-1 tells us that the charge of a proton is $+e$.Thus, Eq. 21-4 gives us

$$
\begin{align*}
F & =\frac{1}{4 \pi \varepsilon_{0}} \frac{e^{2}}{r^{2}} \\
& =\frac{\left(8.99 \times 10^{9} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{C}^{2}\right)\left(1.602 \times 10^{-19} \mathrm{C}\right)^{2}}{\left(4.0 \times 10^{-15} \mathrm{~m}\right)^{2}} \\
& =14 \mathrm{~N} . \tag{Answer}
\end{align*}
$$

(b) What is the magnitude of the gravitational force be-
tween those same two protons?

$$
\begin{aligned}
F & =G \frac{m_{\mathrm{p}}^{2}}{r^{2}} \\
& =\frac{\left(6.67 \times 10^{-11} \mathrm{~N} \cdot \mathrm{~m}^{2} / \mathrm{kg}^{2}\right)\left(1.67 \times 10^{-27} \mathrm{~kg}\right)^{2}}{\left(4.0 \times 10^{-15} \mathrm{~m}\right)^{2}} \\
& =1.2 \times 10^{-35} \mathrm{~N} .
\end{aligned}
$$

## WORKED EXERCISES

1. How many electrons would be removed from a metal to have a charge of $4.8 \mu \mathrm{C}$ ?

Solution
We know that the electric charge is quantized and defined by the equation

$$
\begin{gathered}
q=n e \\
n=\frac{q}{e}=\frac{4.8 \times 10^{-6}}{1.6 \times 10^{-19}}=3.0 \times 10^{13} \text { electrons }
\end{gathered}
$$

## WORKER EXERCISES

2. $5 \times 10^{20}$ electrons pass between two points in 4 s , calculate the current.

Solution
We know that the current is the rate of change of charge, therefore

$$
i=\frac{d q}{d t}=\frac{q}{t}
$$

But the charge is

$$
\begin{gathered}
q=n e \\
i=\frac{n e}{t}=\frac{5 \times 10^{20} \times 1.6 \times 10^{-19}}{4}=20 \mathrm{~A}
\end{gathered}
$$

## WORKED EXERCISES

3. Two charges $4 \mu \mathrm{C}$ and $-3 \mu \mathrm{C}$ are separated by 2 cm . Calculate the force between them ?

Solution
Since the signs of the charges are different, they produce an attractive force. The magnitude of this force is

$$
\begin{gathered}
F=\frac{k\left|q_{1}\right|\left|q_{2}\right|}{r^{2}} \\
F=\frac{9 \times 10^{9} \times 4 \times 10^{-6} \times 3 \times 10^{-6}}{0.02^{2}}=270 \mathrm{~N}
\end{gathered}
$$

## WORKED EXERCISES

4. Calculate the distance between two point charges $2.4 \mu \mathrm{C}$ and $-1.8 \mu \mathrm{C}$ for the electrostatic force to be of magnitude 10.8 N ?

Solution
The magnitude of the electrostatic force is given by

$$
\begin{gathered}
F=\frac{k\left|q_{1}\right|\left|q_{2}\right|}{r^{2}} \quad \rightarrow \quad r=\sqrt{\frac{k\left|q_{1}\right|\left|q_{2}\right|}{F}} \\
r=\sqrt{\frac{k\left|q_{1}\right|\left|q_{2}\right|}{F}}=\sqrt{\frac{9 \times 10^{9} \times 2.4 \times 10^{-6} \times 1.8 \times 10^{-6}}{10.8}}=0.06 \mathrm{~m}=6 \mathrm{~cm}
\end{gathered}
$$

## WORKED EXERCISES

5. A point charge $2.0 \mu \mathrm{C}$ is placed at a distance 4 cm form another point charge q . If the attractive force between them is 56.25 N , find q .

Solution
The magnitude of the electrostatic force is given by

$$
\begin{gathered}
F=\frac{k\left|q_{1}\right|\left|q_{2}\right|}{r^{2}} \rightarrow q_{2}=\frac{F r^{2}}{k q_{1}} \\
q_{2}=\frac{56.25 \times 0.04^{2}}{9 \times 10^{9} \times 2.0 \times 10^{-6}}=5.0 \times 10^{-6} \mathrm{C}=5 \mu C
\end{gathered}
$$

Since the force is ATTRACTIVE, the signs of the charges are DIFFERENT. Therefore the unknown charge is negative $-5.0 \mu \mathrm{C}$.

## Workep Exercises

6. Three point charges $2.0,3.0$, and $-4.0 \mu \mathrm{C}$ are located as shown in the figure. Find the magnitude of the force acting on the $2 \mu \mathrm{C}$ charge due to the others .

Solution


Since the signs of charges ( $2 \mu \mathrm{C}$ and $3 \mu \mathrm{C}$ ) are similar, the force is repulsive. That means the force will be to left and its magnitude is

$$
F_{12}=\frac{9 \times 10^{9} \times 2 \times 10^{-6} \times 3 \times 10^{-6}}{2^{2}}=0.0135 \mathrm{~N}
$$

## WORKER EXERCISES

Since the signs of charges ( $2 \mu \mathrm{C}$ and $-4 \mu \mathrm{C}$ ) are dissimilar, the force is attractive. That means the force will be to right and its magnitude is

$$
F_{13}=\frac{9 \times 10^{9} \times 2 \times 10^{-6} \times 4 \times 10^{-6}}{5^{2}}=0.00288 \mathrm{~N}
$$

Therefore the magnitude of the force on the $2 \mu \mathrm{C}$ particle due to the other charged particles is

$$
F=\left|F_{12}-F_{13}\right|=|0.0135-0.00288|=0.01062 \mathrm{~N}
$$

## WORKED EXERCISES

1. I nree point charges 1.U, $\mathbf{L . U}$, and $5 . \cup \mu \mathrm{C}$ are arranged as snown in the figure. Find the magnitude of the force acting on the $2 \mu \mathrm{C}$ charge due to the others .

Solution

Since the signs of charges ( $1 \mu \mathrm{C}$ and $2 \mu \mathrm{C}$ ) are similar, the force will be up along the positive $y$-direction with magnitude of

$$
F_{12}=\frac{9 \times 10^{9} \times 1 \times 10^{-6} \times 2 \times 10^{-6} 4 \mathrm{~m} 0.002 \mathrm{~N}}{3 \mathrm{3}+\mathrm{Cl}}
$$

## WORKER EXERCISES

Since the signs of charges ( $2 \mu \mathrm{C}$ and $3 \mu \mathrm{C}$ ) are also similar, the force will have two components (one along x and other along y

$$
\begin{aligned}
& F_{13 x}=\frac{9 \times 10^{9} \times 2 \times 10^{-6} \times 3 \times 10^{-6}}{5^{2}} \cdot \frac{4}{5}=0.00173 \mathrm{~N} \\
& F_{13 y}=\frac{9 \times 10^{9} \times 2 \times 10^{-6} \times 3 \times 10^{-6}}{5^{2}} \cdot \frac{3}{5}=0.0013 \mathrm{~N}
\end{aligned}
$$

Therefore the magnitude of the force on the $2 \mu \mathrm{C}$ particle due to the other charged particles is

$$
\begin{gathered}
F_{x}=0.00173 \mathrm{~N} \\
F_{y}=0.002+0.0013=0.0033 \mathrm{~N} \\
F=\sqrt{F_{x}^{2}+F_{y}^{2}}=0.00372 \mathrm{~N}
\end{gathered}
$$

## WORKED EXERCISES

8. Two charges 9.0 and $16.0 \mu \mathrm{C}$ are separated by a distance of 2 m . Where should a third charge $2 \mu \mathrm{C}$ be placed for a net force on it zero?

## Solution

As the charges are of same sign, the third charge must be placed between them and close to the smaller charge in order to have a zero net force.


## WORKED EXERCISES

$$
\frac{9}{x^{2}}=\frac{16}{(2-x)^{2}}
$$

Taking the square root of the above, we get

$$
\frac{3}{x}=\frac{4}{2-x}
$$

This leads to

$$
x=\frac{6}{7}=0.86 \mathrm{~m}
$$

## WORKED EXERCISES

9. Four identical charges $(2 \mu \mathrm{C})$ are located at the vertices of a square of side 5 cm . Calculate the magnitude of the electric force on a $5 \mu \mathrm{C}$ located at the center of the square.

## Solution

The electric forces on the $5 \mu \mathrm{C}$ due to the other charges have the same magnitude. Each charge along the diagonal will experience equal and opposite force on the $5 \mu \mathrm{C}$ charge, therefore, the resultant force is zero.


