

CHAPTER 4

section 4.2

4) $y' = 2x^9 + 1$

25) $\frac{d}{dx}(fg)|_{x=-2} = 24$

$$\frac{d}{dx}\left(\frac{f}{g}\right)|_{x=-2} = \frac{18}{49}$$

$$\frac{d}{dx}\left(\frac{g}{f}\right)|_{x=-2} = -18$$

$$\frac{d}{dx}(2f - 3g)|_{x=-2} = -3$$

section 4.4

20) $y'' = \frac{2}{x^3}$

section 4.5

10) $y' = \frac{5}{4} \sec^{\frac{5}{4}}(x+5) \tan(x+5)$

19) using the logarithmic differentiation

$$y' = \left(\frac{x^2-1}{x^3+1}\right)^4 \left(\frac{8x}{x^2-1} - \frac{12x^2}{x^3+1}\right)$$

using chain rule and quotient rule

$$\begin{aligned} y' &= 4 \left(\frac{x^2-1}{x^3+1}\right)^3 \left(\frac{-x^4+3x^2+2x}{(x^3+1)^2}\right) \\ &= \frac{4(x^2-1)^3(-x^4+3x^2+2x)}{(x^3+1)^5} \end{aligned}$$

section 4.6

25) The equation of the tangent line is

$$y = 4x + 8$$

The equation of the normal line is

$$y = \frac{-1}{4}x + \frac{15}{4}$$

section 4.7

20) $y' = x^x (1 + \ln x)$

21) $y' = \left(\frac{\sin^2 x \tan^4 x}{(x^2 + 1)^2} \right) \left(2 \cot x + 4 \cot x \sec^2 x - \frac{4x}{x^2 + 1} \right)$

24) $y' = x^{\cos x} \left(\frac{\cos x - x \ln x \sin x}{x} \right)$

26) $y' = (\sin x)^x (x \cot x + \ln(\sin x))$
