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**Text Book:**

Dennis G. Zill and Patrick D. Shanahan, Complex Analysis, 1<sup>st</sup> edition, Jones & Barlett Learning, 2003

**Office Hours:**

**Grading:**

| <b>Assessment</b> | <b>Type of assessment</b> | <b>Time</b> | <b>Grade</b> |
|-------------------|---------------------------|-------------|--------------|
| Exam 1            | Written exam              | Week 6      | 20           |
| Open book Exam    | Written exam              | Week 10     | 10           |
| Exam 2            | Written exam              | Week 11     | 20           |
| Report            | Writing a report          |             | 10           |
| Final Exam        | Written exam              | Week 15     | 40           |

**Material Covered:**

**Chapter 1.**

**Complex Numbers and the Complex Plane**

- 1.1 Complex Numbers and Their Properties
- 1.2 Complex Plane
- 1.3 Polar Form of Complex Numbers
- 1.4 Powers and Roots
- 1.5 Sets of Points in the Complex Plane

**Chapter 2.**

**Complex Functions and Mappings**

- 2.1 Complex Functions
- 2.2 Complex Functions as Mappings
- 2.3 Linear Mappings
- 2.4 Special Power Functions
  - 2.4.1 The Power Function  $z^n$
  - 2.4.2 The Power Function  $z^{1/n}$
- 2.5 Reciprocal Function
- 2.6 Limits and Continuity
  - 2.6.1 Limits
  - 2.6.2 Continuity

## **Chapter 3.**

### **Analytic Functions**

- 3.1 Differentiability and Analyticity
- 3.2 Cauchy-Riemann Equations
- 3.3 Harmonic Functions

## **Chapter 4.**

### **Elementary Functions**

- 4.1 Exponential and Logarithmic Functions
  - 4.1.1 Complex Exponential Function
  - 4.1.2 Complex Logarithmic Function
- 4.2 Complex Powers
- 4.3 Trigonometric and Hyperbolic Functions
  - 4.3.1 Complex Trigonometric Functions
  - 4.3.2 Complex Hyperbolic Functions

## **Chapter 5.**

### **Integration in the Complex Plane**

- 5.2 Complex Integrals
- 5.3 Cauchy-Goursat Theorem
- 5.4 Independence of Path
- 5.5 Cauchy's Integral Formulas and Their Consequences
  - 5.5.1 Cauchy's Two Integral Formulas

## **Chapter 6.**

### **Series and Residues**

- 6.2 Taylor Series
- 6.3 Laurent Series
- 6.4 Zeros and Poles
- 6.5 Residues and Residue Theorem

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### Chapter 1

| Section | Example   | Read                             | Exercise                                     |
|---------|-----------|----------------------------------|--|
| 1.1     | 1 , 2 , 3 | 47, 50, 51.                      | 1, 3-11 , 15,17,19, 25,26, 27,29, 31, 35,45. |
| 1.2     | 1 , 2     | Example 3<br>33, 34, 36, 37, 38. | 1, 3, 8, 9, 11, 13, 15, 17, 19, 27, 31.      |
| 1.3     | 1,2,3,4   | 40,43,44,45.                     | 1,3,5,9,11,13,14,15,19,25,29,31,33,37(a)     |
| 1.4     | 1         | Example 2,21,<br>27.             | 1,4,5,9,15,17,19(a,b)                        |
| 1.5     | 1,2       | 35,39,40,<br>43(a,c,e),44        | 1,3,5,13,17,21,23,25,27,30                   |

## Chapter 2

| Section | Example       | Read                                     | Exercise  |
|---------|---------------|--|---|
| 2.1     | 1,2           | 27(a,b,d,e),28(a,b,c),<br>29a,32(a,c),35 | 1(a,b,c),2(a,b),6b,<br>7(a,b)<br>9,11,15,21,23,25 |
| 2.2     | 1,3,4         | 2  | 1,3,5,9,11,17,19,23,25                            |
| 2.4.1   | 1             | Example(2,3)                             | 1, 5,7,<br>9,15,17,21.                            |
| 2.4.2   | 5(a,b),9(a,b) | Example(5c,8)                            | 25,29,31,33,43.                                   |
| 2.6.1   | 1,2,3,4       | 4,13                                     | 1,4,5,7,11,13                                     |
| 2.6.2   | 5,7           | 39,45,46                                 | 27,31,35  |

### **Chapter 3**

| <b>Section</b> | <b>Example</b> | <b>Read</b> | <b>Exercise</b>                   |
|----------------|----------------|-------------|-----------------------------------|
| <b>3.1</b>     | <b>1,2,3</b>   | <b>32</b>   | <b>1,3,5,11,17,19,32</b>          |
| <b>3.2</b>     | <b>1,2,3</b>   |             | <b>1,3,5,9,17,19,23<br/>25,27</b> |
| <b>3.3</b>     | <b>1,2</b>     | <b>18</b>   | <b>3,7,9,11</b>                   |

**Chapter 4**  
**Self-study**  
(30min dissection-1hr open-book exam, 10 marks)

| Section | Example   | Read | Exercise                  |
|---------|-----------|------|---------------------------|
| 4.1     | 1,2,3,4,5 |      | 1,3,5,9,13,21,23,29,33,48 |
| 4.2     | 1,2,3     |      | 1,5,9,17                  |
| 4.3     | 1         |      | 1,3,5                     |

- without the concept of mapping for all functions

## Chapter 5

| <b>Section</b> | <b>Example</b> | <b>Read</b>   | <b>Exercise</b>        |
|----------------|----------------|---------------|------------------------|
| 5.2            | 1,2,3,4        | 9             | 1,3,5,7,11,17,21,23,25 |
| 5.3            | 1,2,3,4,5      | 27(a,b),28(a) | 1,3,9,11,15,17,19      |
| 5.4            | 1,4,5          | Example(2,3)  | 3,5,9,11,13,15,17      |
| 5.5.1          | 1,2,3          | Example4,28   | 1,3,7,11,15,17,20,21   |

**Chapter 6**

| <b>Section</b> | <b>Example</b> | <b>Read</b>   | <b>Exercise</b>                |
|----------------|----------------|---------------|--------------------------------|
| 6.2            | 1,2            | 9,40          | 1,5,13,15,19,21                |
| 6.3            | 1,2,4,6        | Example (3,5) | 4,5,7,11,13,17,21,25,27        |
| 6.4            | 1,2,3,4        | 31            | 1,3,5,9,13,15,21,25,27,29      |
| 6.5            | 1,2,3,4,5,6,8  | Example7,36   | 1,3,5,7,9,13,15,17,21,25,27,31 |