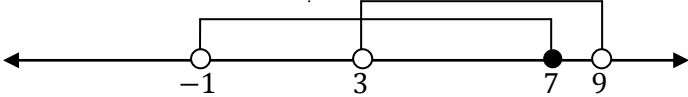
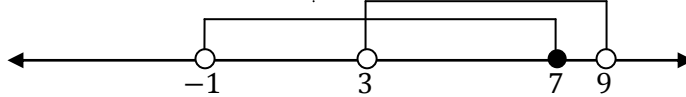
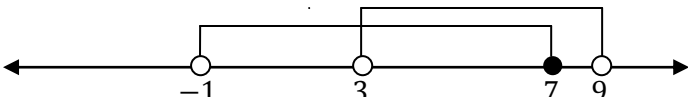


## Workshop Solutions to Sections 1.1 and 1.2

1) $\{x \in \mathbb{R}   -3 \leq x \leq 3\} = [-3, 3]$	2) $\{x \in \mathbb{R}   -2 < x < 5\} = (-2, 5)$
3) $\{x \in \mathbb{R}   -2 < x \leq 5\} = (-2, 5]$	4) $\{x \in \mathbb{R}   -3 \leq x < 3\} = [-3, 3)$
5) $\{x \in \mathbb{R}   x \leq -2\} = (-\infty, -2]$	6) $\{x \in \mathbb{R}   x > -2\} = (-2, \infty)$
7) $(-1, 7] \setminus (3, 9) =$ <u>Solution:</u>  $(-1, 7] \setminus (3, 9) = (-1, 3] = \{x \in \mathbb{R}   -1 < x \leq 3\}$	8) $(-1, 7] \cup (3, 9) =$ <u>Solution:</u>  $(-1, 7] \cup (3, 9) = (-1, 9) = \{x \in \mathbb{R}   -1 < x < 9\}$
9) $(-1, 7] \cap (3, 9) =$ <u>Solution:</u>  $(-1, 7] \cap (3, 9) = (3, 7] = \{x \in \mathbb{R}   3 < x \leq 7\}$	10) $ -7.2  = -(-7.2) = 7.2$
	11) $ 0.14 - \pi  =  0.14 - 3.14  =  -3  = 3$ <b>OR</b> $ 0.14 - \pi  = -(0.14 - \pi) = \pi - 0.14$
	12) $ 2 - \pi  = -(2 - \pi) = \pi - 2$
13) $ \pi - 2  = \pi - 2$	14) The solution of the inequality $-3x + 5 < -13$ is <u>Solution:</u> $\begin{aligned} -3x + 5 &< -13 \\ -3x &< -13 - 5 \\ -3x &< -18 \\ \frac{-3x}{-3} &> \frac{-18}{-3} \\ x &> 6 \end{aligned}$ The solution set is $(6, \infty) = \{x \in \mathbb{R}   x > 6\}$ .
15) The solution of the inequality $11 > 5 - 3x \geq -13$ is <u>Solution:</u> $\begin{aligned} 11 &> 5 - 3x \geq -13 \\ 11 - 5 &> -3x \geq -13 - 5 \\ 6 &> -3x \geq -18 \\ \frac{6}{-3} &< \frac{-3x}{-3} \leq \frac{-18}{-3} \\ -2 &< x \leq 6 \end{aligned}$ The solution set is $(-2, 6] = \{x \in \mathbb{R}   -2 < x \leq 6\}$ .	16) If $2x + 3 = 1 - 6(x - 1)$ , then $x =$ <u>Solution:</u> $\begin{aligned} 2x + 3 &= 1 - 6(x - 1) \\ 2x + 3 &= 1 - 6x + 6 \\ 2x + 6x &= 1 + 6 - 3 \\ 8x &= 4 \\ x &= \frac{4}{8} \\ x &= \frac{1}{2} \end{aligned}$

17) The solution of the inequality  $x^2 - 5x + 6 > 0$  is  
Solution:

$$x^2 - 5x + 6 > 0$$

$$\Leftrightarrow (x - 2)(x - 3) > 0$$

The transition points are 2 and 3. We should now investigate the sign of  $(x - 2)(x - 3)$  where is  $> 0$ .

2                      3

Sign of $(x - 2)(x - 3)$	+++	---	+++
Solution	Yes	No	Yes

The solution set is  $(-\infty, 2) \cup (3, \infty)$ .

18) The solution of the inequality  $x^2 - 5x + 6 \geq 0$  is  
Solution:

$$x^2 - 5x + 6 \geq 0$$

$$\Leftrightarrow (x - 2)(x - 3) \geq 0$$

The transition points are 2 and 3. We should now investigate the sign of  $(x - 2)(x - 3)$  where is  $\geq 0$ .

2                      3

Sign of $(x - 2)(x - 3)$	+++	---	+++
Solution	Yes	No	Yes

The solution set is  $(-\infty, 2] \cup [3, \infty)$ .

19) The solution of the inequality  $x^2 - 5x + 6 \leq 0$  is  
Solution:

$$x^2 - 5x + 6 \leq 0$$

$$\Leftrightarrow (x - 2)(x - 3) \leq 0$$

The transition points are 2 and 3. We should now investigate the sign of  $(x - 2)(x - 3)$  where is  $\leq 0$ .

2                      3

Sign of $(x - 2)(x - 3)$	+++	---	+++
Solution	No	Yes	No

The solution set is  $[2, 3]$ .

20) The solution of the inequality  $x^2 - 5x < -6$  is  
Solution:

$$x^2 - 5x < -6$$

$$x^2 - 5x + 6 < 0$$

$$\Leftrightarrow (x - 2)(x - 3) < 0$$

The transition points are 2 and 3. We should now investigate the sign of  $(x - 2)(x - 3)$  where is  $< 0$ .

2                      3

Sign of $(x - 2)(x - 3)$	+++	---	+++
Solution	No	Yes	No

The solution set is  $(2, 3)$ .

21) The solution of the inequality  $x^2 - x \geq 2$  is  
Solution:

$$x^2 - x \geq 2$$

$$x^2 - x - 2 \geq 0$$

$$\Leftrightarrow (x - 2)(x + 1) \geq 0$$

The transition points are -1 and 2. We should now investigate the sign of  $(x - 2)(x + 1)$  where is  $\geq 0$ .

-1                      2

Sign of $(x - 2)(x + 1)$	+++	---	+++
Solution	Yes	No	Yes

The solution set is  $(-\infty, -1] \cup [2, \infty)$ .

22) The solution of the inequality  $x^2 - x \leq 2$  is  
Solution:

$$x^2 - x \leq 2$$

$$x^2 - x - 2 \leq 0$$

$$\Leftrightarrow (x - 2)(x + 1) \leq 0$$

The transition points are -1 and 2. We should now investigate the sign of  $(x - 2)(x + 1)$  where is  $\leq 0$ .

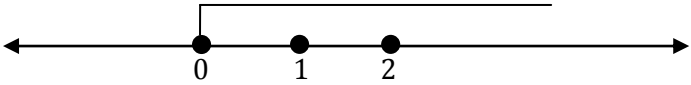
-1                      2

Sign of $(x - 2)(x + 1)$	+++	---	+++
Solution	No	Yes	No

The solution set is  $[-1, 2]$ .

<p>23) The solution of the inequality <math>x^2 - x &gt; 2</math> is</p> <p><u>Solution:</u></p> $x^2 - x > 2$ $x^2 - x - 2 > 0$ $\Leftrightarrow (x - 2)(x + 1) > 0$ <p>The transition points are <math>-1</math> and <math>2</math>. We should now investigate the sign of <math>(x - 2)(x + 1)</math> where is <math>&gt; 0</math>.</p> <table><tr><td>Sign of <math>(x - 2)(x + 1)</math></td><td>+++</td><td>---</td><td>+++</td></tr><tr><td>Solution</td><td>Yes</td><td>No</td><td>Yes</td></tr></table> <p>The solution set is <math>(-\infty, -1) \cup (2, \infty)</math>.</p>	Sign of $(x - 2)(x + 1)$	+++	---	+++	Solution	Yes	No	Yes	<p>24) If <math> 3x - 7  = 2</math>, then <math>x =</math></p> <p><u>Solution:</u></p> $ 3x - 7  = 2$ $3x - 7 = 2 \quad \text{or} \quad 3x - 7 = -2$ $3x = 2 + 7 \quad \text{or} \quad 3x = -2 + 7$ $3x = 9 \quad \text{or} \quad 3x = 5$ $x = \frac{9}{3} \quad \text{or} \quad x = \frac{5}{3}$ $x = 3 \quad \text{or} \quad x = \frac{5}{3}$
Sign of $(x - 2)(x + 1)$	+++	---	+++						
Solution	Yes	No	Yes						
<p>25) If <math> x - 4  = 3</math>, then <math>x =</math></p> <p><u>Solution:</u></p> $ x - 4  = 3$ $x - 4 = 3 \quad \text{or} \quad x - 4 = -3$ $x = 3 + 4 \quad \text{or} \quad x = -3 + 4$ $x = 7 \quad \text{or} \quad x = 1$	<p>26) The solution of the inequality <math> x - 3  &lt; 4</math> is</p> <p><u>Solution:</u></p> $ x - 3  < 4$ $-4 < x - 3 < 4$ $-4 + 3 < x < 4 + 3$ $-1 < x < 7$ <p>The solution set is <math>(-1, 7) = \{x \in \mathbb{R}   -1 &lt; x &lt; 7\}</math>.</p>								
<p>27) The solution of the inequality <math> x - 3  \leq 4</math> is</p> <p><u>Solution:</u></p> $ x - 3  \leq 4$ $-4 \leq x - 3 \leq 4$ $-4 + 3 \leq x \leq 4 + 3$ $-1 \leq x \leq 7$ <p>The solution set is <math>[-1, 7] = \{x \in \mathbb{R}   -1 \leq x \leq 7\}</math>.</p>	<p>28) The solution of the inequality <math> x - 3  &gt; 4</math> is</p> <p><u>Solution:</u></p> $ x - 3  > 4$ $x - 3 > 4 \quad \text{or} \quad x - 3 < -4$ $x > 4 + 3 \quad \text{or} \quad x < -4 + 3$ $x > 7 \quad \text{or} \quad x < -1$ <p>The solution set is <math>(-\infty, -1) \cup (7, \infty)</math>.</p>								
<p>29) The solution of the inequality <math> x - 3  \geq 4</math> is</p> <p><u>Solution:</u></p> $ x - 3  \geq 4$ $x - 3 \geq 4 \quad \text{or} \quad x - 3 \leq -4$ $x \geq 4 + 3 \quad \text{or} \quad x \leq -4 + 3$ $x \geq 7 \quad \text{or} \quad x \leq -1$ <p>The solution set is <math>(-\infty, -1] \cup [7, \infty)</math>.</p>	<p>30) The distance between the real numbers <math>-5</math> and <math>6</math> is</p> <p><u>Solution:</u></p> <p>The distance <math>(d) =  (-5) - (6)  =  -11  = -(-11) = 11</math></p>								
<p>31) The distance between the real numbers <math>\frac{15}{8}</math> and <math>\frac{23}{12}</math> is</p> <p><u>Solution:</u></p> <p>The distance <math>(d) = \left  \left( \frac{15}{8} \right) - \left( \frac{23}{12} \right) \right  = \left  \frac{45 - 46}{24} \right </math></p> $= \left  -\frac{1}{24} \right  = -\left( -\frac{1}{24} \right) = \frac{1}{24}$	<p>32) The distance between the points <math>(-2, -5)</math> and <math>(3, 1)</math> is</p> <p><u>Solution:</u></p> $d = \sqrt{(-2 - 3)^2 + (-5 - 1)^2} = \sqrt{(-5)^2 + (-6)^2}$ $= \sqrt{25 + 36} = \sqrt{61}$								
<p>33) The distance between the pairs <math>(-2, 5)</math> and <math>(1, 1)</math> is</p> <p><u>Solution:</u></p> $d = \sqrt{(-2 - 1)^2 + (5 - 1)^2} = \sqrt{(-3)^2 + (4)^2}$ $= \sqrt{9 + 16} = \sqrt{25} = 5$	<p>34) If <math>x^2 - 3x = 4</math>, then <math>x =</math></p> <p><u>Solution:</u></p> <p>First, we write <math>x^2 - 3x - 4 = 0</math></p> $\Rightarrow (x - 4)(x + 1) = 0$ $\Rightarrow x - 4 = 0 \quad \text{or} \quad x + 1 = 0$ $\Rightarrow x = 4 \quad \text{or} \quad x = -1$								

<p>35) If <math>3x^2 - 6 = 0</math>, then <math>x =</math>  <u>Solution:</u></p> $\begin{aligned} 3x^2 - 6 &= 0 \\ \Rightarrow 3x^2 &= 6 \\ \Rightarrow x^2 &= \frac{6}{3} \\ \Rightarrow x^2 &= 2 \\ \Rightarrow x &= \pm\sqrt{2} \end{aligned}$	<p>36) If <math>x(x - 5) = 14</math>, then <math>x =</math>  <u>Solution:</u>  First, we write <math>x(x - 5) = 14</math></p> $\begin{aligned} \Rightarrow x^2 - 5x &= 14 \\ \Rightarrow x^2 - 5x - 14 &= 0 \\ \Rightarrow (x - 7)(x + 2) &= 0 \\ \Rightarrow x - 7 = 0 \quad \text{or} \quad x + 2 = 0 \\ \Rightarrow x = 7 \quad \text{or} \quad x = -2 \end{aligned}$
<p>37) The solution of the equation  <math>3(x - 2) = 2(x + 1) + 7</math> is  <u>Solution:</u></p> $\begin{aligned} 3(x - 2) &= 2(x + 1) + 7 \\ 3x - 6 &= 2x + 2 + 7 \\ 3x - 2x &= 2 + 7 + 6 \\ x &= 15 \end{aligned}$	<p>38) The solution of the equation  <math>2x + 3 = \frac{x}{2} + 9</math> is  <u>Solution:</u></p> $\begin{aligned} 2x + 3 &= \frac{x}{2} + 9 \\ 4x + 6 &= x + 18 \\ 4x - x &= 18 - 6 \\ 3x &= 12 \\ x &= 4 \end{aligned}$
<p>39) If <math>x^2 + 25 = 10x</math>, then <math>x =</math>  <u>Solution:</u></p> $\begin{aligned} x^2 + 25 &= 10x \\ x^2 - 10x + 25 &= 0 \\ (x - 5)(x - 5) &= 0 \\ x &= 5 \quad (\text{repeated}) \end{aligned}$	<p>40) If <math>x^2 - 36 = 0</math>, then <math>x =</math>  <u>Solution:</u></p> $\begin{aligned} x^2 - 36 &= 0 \\ x^2 &= 36 \\ x &= \pm\sqrt{36} \\ x &= \pm 6 \end{aligned}$
<p>41) If <math>9(2x + 8) = 20 - (x + 5)</math>, then <math>x =</math>  <u>Solution:</u></p> $\begin{aligned} 9(2x + 8) &= 20 - (x + 5) \\ 18x + 72 &= 20 - x - 5 \\ 18x + x &= 20 - 5 - 72 \\ 19x &= -57 \\ x &= -\frac{57}{19} \\ x &= -3 \end{aligned}$	<p>42) If <math>2(x - 5) + 8 = 5x + 3</math>, then <math>x =</math>  <u>Solution:</u></p> $\begin{aligned} 2(x - 5) + 8 &= 5x + 3 \\ 2x - 10 + 8 &= 5x + 3 \\ 2x - 5x &= 3 - 8 + 10 \\ -3x &= 5 \\ x &= -\frac{5}{3} \end{aligned}$
<p>43) The solution of the equation  <math>2x^2 - 3x = 5</math> is  <u>Solution:</u></p> $\begin{aligned} 2x^2 - 3x &= 5 \\ 2x^2 - 3x - 5 &= 0 \\ a &= 2, \quad b = -3, \quad c = -5 \\ x_{1,2} &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-(-3) \pm \sqrt{(-3)^2 - 4(2)(-5)}}{2(2)} \\ &= \frac{3 \pm \sqrt{9 + 40}}{4} = \frac{3 \pm \sqrt{49}}{4} = \frac{3 \pm 7}{4} \\ \therefore x_1 &= \frac{3 + 7}{4} = \frac{10}{4} = \frac{5}{2} \\ x_2 &= \frac{3 - 7}{4} = \frac{-4}{4} = -1 \end{aligned}$ <p>Therefore, the solution of the equation is  <math>x = -1</math> or <math>x = \frac{5}{2}</math></p>	<p>44) The solution of the equation  <math>x^3 - 2x^2 - 3x = 0</math> is  <u>Solution:</u></p> $\begin{aligned} x^3 - 2x^2 - 3x &= 0 \\ x(x^2 - 2x - 3) &= 0 \\ x(x + 1)(x - 3) &= 0 \\ \Leftrightarrow x = 0 \quad \text{or} \quad x + 1 = 0 \quad \text{or} \quad x - 3 = 0 \\ \Leftrightarrow x = 0 \quad \text{or} \quad x = -1 \quad \text{or} \quad x = 3 \end{aligned}$

<p>45) The solution of the equation <math>4x = \frac{2x+1}{3} - 2</math> is</p> <p><u>Solution:</u></p> $4x = \frac{2x+1}{3} - 2$ $12x = (2x+1) - 6$ $12x = 2x+1-6$ $12x-2x = 1-6$ $10x = -5$ $x = \frac{-5}{10}$ $x = -\frac{1}{2}$	<p>46) The solution of the equation <math>x^4 + x^3 - 2x^2 = 0</math> is</p> <p><u>Solution:</u></p> $x^4 + x^3 - 2x^2 = 0$ $x^2(x^2 + x - 2) = 0$ $x^2(x+2)(x-1) = 0$ $\Leftrightarrow x^2 = 0 \text{ or } x+2 = 0 \text{ or } x-1 = 0$ $\Leftrightarrow x = 0 \text{ (repeated) or } x = -2 \text{ or } x = 1$
<p>47) The solution of the equation <math>6x^2 + x = 2</math> is</p> <p><u>Solution:</u></p> $6x^2 + x = 2$ $6x^2 + x - 2 = 0$ $a = 6, b = 1, c = -2$ $x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(1) \pm \sqrt{(1)^2 - 4(6)(-2)}}{2(6)}$ $= \frac{-1 \pm \sqrt{1+48}}{12} = \frac{-1 \pm \sqrt{49}}{12} = \frac{-1 \pm 7}{12}$ $\therefore x_1 = \frac{-1+7}{12} = \frac{6}{12} = \frac{1}{2}$ $x_2 = \frac{-1-7}{12} = \frac{-8}{12} = -\frac{2}{3}$ <p>Therefore, the solution of the equation is</p> $x = -\frac{2}{3} \text{ or } x = \frac{1}{2}$	<p>48) The solution of the equation <math>2x^2 + 3 = -7x</math> is</p> <p><u>Solution:</u></p> $2x^2 + 3 = -7x$ $2x^2 + 7x + 3 = 0$ $a = 2, b = 7, c = 3$ $x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(7) \pm \sqrt{(7)^2 - 4(2)(3)}}{2(2)}$ $= \frac{-7 \pm \sqrt{49-24}}{4} = \frac{-7 \pm \sqrt{25}}{4}$ $= \frac{-7 \pm 5}{4}$ $\therefore x_1 = \frac{-7+5}{4} = \frac{-2}{4} = -\frac{1}{2}$ $x_2 = \frac{-7-5}{4} = \frac{-12}{4} = -3$ <p>Therefore, the solution of the equation is</p> $x = -\frac{1}{2} \text{ or } x = -3$
<p>49) <math>[0, \infty) \setminus \{1, 2\} =</math></p> <p><u>Solution:</u></p>  $[0, \infty) \setminus \{1, 2\} = [0, 1) \cup (1, 2) \cup (2, \infty).$	<p>50) The integer in <math>\mathbb{Z}</math> is <math>\sqrt{25} = 5</math>.</p> <p>51) The rational in <math>\mathbb{Q}</math> is <math>\frac{2}{3}</math>.</p> <p>52) The irrational in <math>\mathbb{I}</math> is <math>\sqrt{2}</math>.</p>