

Solution

1. A proton, moving with a speed of 4×10^6 m/s through a magnetic field of 1.15 T, experiences a magnetic force of 6.4×10^{-13} N. Determine the angle between the proton's velocity and the magnetic field.

The magnetic force is defined as

$$\vec{F} = q \vec{v} \times \vec{B}$$

Hence the magnitude of the magnetic field is given as

$$F = qvB \sin\theta$$

Therefore the angle is

$$\sin\theta = \frac{F}{qvB} = \frac{6.4 \times 10^{-13}}{1.6 \times 10^{-19} \times 4 \times 10^6 \times 1.15} = 0.869$$

$$\theta = 60.4^\circ$$

1. A 2 eV proton rotates in a circle, of radius 4.2 cm, under the influence of a uniform magnetic field. Calculate the magnitude of the magnetic field.

The radius of the curvature is

$$R = \frac{mv}{qB} \rightarrow B = \frac{mv}{qR}$$

From the kinetic energy we get

$$K = \frac{1}{2}mv^2 \rightarrow v = \sqrt{\frac{2K}{m}} = \sqrt{\frac{2 \times 2 \times 1.6 \times 10^{-19}}{1.67 \times 10^{-27}}} = 1.96 \times 10^4 \text{ m/s}$$

Therefore the magnitude of the magnetic field is

$$B = \frac{mv}{qR} = \frac{1.67 \times 10^{-27} \times 1.96 \times 10^4}{1.6 \times 10^{-19} \times 4.2 \times 10^{-2}} = 4.9 \text{ mT}$$