

Solution

Q1 [3 MARKS]: A charge q is located 4 cm from another charge of -5 nC. If the repulsive force created between these charges is 2.25×10^{-4} N, what is q ?

It is well known that the magnitude of the electrostatic force is

$$F = \frac{k q_1 q_2}{r^2}$$

Therefore

$$q_2 = \frac{F r^2}{k q_1} = \frac{2.25 \times 10^{-4} \times 0.04^2}{9.0 \times 10^9 \times 5.0 \times 10^{-9}} = 8.0 \times 10^{-9} \text{ C}$$

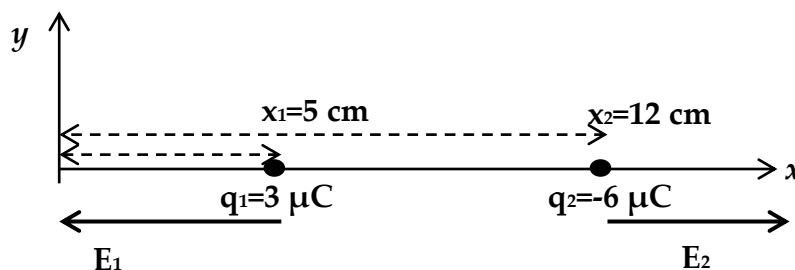
Since the electrostatic force is *repulsive*, both charges have the *same sign*. Hence the unknown charge is

$$q_2 = -8.0 \times 10^{-9} \text{ C}$$

Q2 [4+3 MARKS]: Two point charges are located on the x -axis as following: $q_1 = 3 \mu\text{C}$ at $x = 5$ cm and $q_2 = -6 \mu\text{C}$ at $x = 12$ cm.

(1) Calculate the magnitude and direction of the electric field at the origin $x = 0$.

(2) If a charge $Q = -2$ nC is placed now at the origin, calculate the magnitude and direction of the force acting on this charge [Hint: use the result obtained in (1)].



(1) The electric field due to charge 1 is along the *negative x-axis* and equals

$$E_1 = \frac{k q_1}{r_1^2} = \frac{9.0 \times 10^9 \times 3.0 \times 10^{-6}}{0.05^2} = 10.8 \times 10^6 \text{ N/C}$$

The electric field due to charge 2 is along the *positive x-axis* and equals

$$E_2 = \frac{k q_2}{r_2^2} = \frac{9.0 \times 10^9 \times 6.0 \times 10^{-6}}{0.12^2} = 3.75 \times 10^6 \text{ N/C}$$

Hence the resultant electric field is

$$E = E_2 - E_1 = 3.75 \times 10^6 - 10.8 \times 10^6 = -7.05 \times 10^6 \text{ N/C}$$

The *minus* sign indicates that the resultant electric field directs along the *negative x-axis*.

(2) The magnitude of the electric force is

$$F = QE = 2.0 \times 10^{-9} \times 7.05 \times 10^6 = 0.0141 \text{ N}$$

Since the charge Q is *negative*, the force will oppose the electric field. Therefore the direction of the force is along the *positive x-axis*.